

Statistical Methods Curriculum

Middle Township Public Schools 216 S. Main Street Cape May Court House, NJ 08210

Table of Contents

Acknowledgements	1
Introduction	2
Course Description	3-4
Pacing Guide	5-6
Unit Plans	7-46
Unit 1-Introduction to Statistics 7-10	
Unit 2 – Descriptive Statistics	
Unit 3 – Probability Introduction	
Unit 4- Discrete Probability Distributions	
Unit 5 – Normal Probability Distributions	
Unit 6 – Confidence Intervals27 - 30	
Unit 7 – Hypothesis Testing with One Sample	
Unit 8 – Hypothesis Testing with Two Samples35 - 38	
Unit 9 – Correlation and Regression39 - 42	
Unit 10 – Chi – Square	
Accommodations/Modifications4	7
Resources	

Acknowledgements

Dr. David Salvo Dr. Toni Lehman George West Superintendent Director of Curriculum and Instruction Principal, Middle Township High School

Statistical Methods Curriculum Work Committee

Kelsey Graham

Statistical Methods Course Overview

Statistical Methods is offered to any student who has successfully completed a second-year course in algebra and who possesses sufficient mathematical maturity and quantitative reasoning ability. Students with the appropriate mathematical background are encouraged to take both Statistical Methods and Honors Calculus in High School. There are six themes in the Statistical Methods course: exploring data, sampling and experimentation, anticipating patterns, and statistical inference. Upon completion of this course, students should possess the skills necessary to be successful in subsequent mathematics courses.

Student Learning Outcomes

- 1. STUDENT LEARNING OUTCOME: Student will build frequency distributions and present statistical results graphically.
- 2. STUDENT LEARNING OUTCOME: Student will describe data with descriptive statistics.
- 3. STUDENT LEARNING OUTCOME: Student will apply counting techniques to probability and discrete probability distributions.
- 4. STUDENT LEARNINGOUT COME: Student will construct and employ confidence intervals.
- 5. <u>STUDENT LEARNINGOUTCOME</u>: Student will apply the normal distribution, confidence intervals, sample size, hypothesis testing, analysis of variance, correlation, and regression to obtain statistical results with which they will draw conclusions.
- 6. <u>STUDENT LEARNING OUTCOME</u>: Student will use technology to help solve problems, experiment, analyze results, interpret results, and verify conclusions.

New Jersey State Department of Education

Core Curriculum Content Standards

A note about Mathematics Standards and Cumulative Progress Indicators.

A complete copy of the Core Curriculum Content Standards for Mathematics may also be found at:

NJDOE Mathematics Model Curriculum Grades K-12

http://www.nj.gov/education/modelcurriculum/math/

NJDOE Mathematics Curriculum K-12 pdf

http://www.state.nj.us/education/cccs/2016/math/standards.pdf

Common Core State Standards Initiative -- Mathematics

http://www.corestandards.org/Math/

Statistical Methods

Scope and Sequence

Quarter I					
Unit 1 Introduction to Statistics I. Data classification II. Variable and Data Types III. Data Collection and Experimental Design	Unit 2 Descriptive Statistics: I. Frequency Distributions and their Graphs II. Histograms, Ogive, Stem Plot, Dot Plot, Scatter Plot III. Measures of Central Tendency IV. Measures of Variation V. Measures of Position				
Unit 3 Probability Introduction:					
Basic Concepts of Probability and Counting The Multiplication Rule The Addition Rule					
Quarter II					
Unit 4 Discrete Probability Distributions: I. Probability Distributions II. Binomial Distributions III. Mean, Variance, Standard Distribution, Expectation	Unit 5 Normal Probability Distributions: I. Introduction to Normal Distributions II. Normal Distributions: Probabilities III. Normal Distributions: Finding Values IV. Central Limit Theorem				

Quarter III				
 Unit 6 Confidence Intervals: I. Confidence Intervals for the Mean (σ known) II. Confidence Intervals for the Mean (σ unknown) III. Confidence Intervals for Variance and Standard Deviation Unit 8 Hypothesis Testing with Two Samples: I. Testing the Difference Between Two Means II. Testing the Difference between Two Variances 	Unit 7 Hypothesis testing with One Sample: I. Introduction to Hypothesis Testing II. Hypothesis Testing for a Mean (σ known) III. Hypothesis Testing for a Mean (σ unknown) IV. Hypothesis Testing for a Proportion V. Hypothesis Testing for Variance and Standard Deviation			
Qua	rter IV			
Unit 9 Correlation and Regression: I. Correlation II. Regression	Unit 10 Chi-Square: I. Chi-Square Test II. Analysis of Variance			

Suggested days of	Subject/Grade Level: 11/12	Unit 1: Introduction to Statistics			
Instruction 15 days	Statistical Methods	Topic: Data Collection and Classification			
13 days		Overarching Goals: (1) Communicate mathematical ideas in clear, concise, organized language that varies in content, format and form for different audiences and purposes.			
		(2) Comprehend, understand, analyze, evaluate, critique, solve, and respond to a variety of real-life, meaningful problems. (3) Investigate, research, and synthesize various information from a variety of media sources.			
		Goal 1: The student will be able to use basis of language of statistics while collecting data and classifying the various data types.			
		Student Learning Outcome: Student will describe data with descriptive statistics.			
	Objectives / Cluster Concepts / Cumulative Progress Indicators (CPI's) The student will be able to:	Essential Question(s): What provocative questions will foster inquiry, understanding, and transfer of learning?			

1.1.	Define statistics and its
	branches (i.e. descriptive
	and inferential)
	S-IC A-1

- 1.2. Distinguish data sets s-IC A-2
- 1.3. Types of data, quantitative and qualitative s-ID B-5
- 1.4. Levels of measurement, nominal, ordinal, interval, ratio s-ID B-5
- 1.5. Design of a statistical study S-IC B-3
- 1.6. Data Collection s-IC A-1
- 1.7. Observational Study s-IC B-3
- 1.8. Experimental Design s-IC B-3
- 1.9. Sampling Techniques S-IC B-4

Essential Questions:

- How do you collect and classify data?
- How do you distinguish between descriptive and inferential statistics?
- How do you distinguish between quantitative and qualitative data?
- What are considerations when collecting data, including technique and ethical concerns?
- How do you design a statistical study?
- How do you design a sample with and without bias using various sampling techniques?

Check all that apply.		Indicate whether these skills are E -Encouraged, T -Taught, or A -Assessed in this unit by markin T , A on the line before the appropriate skill.		
	21 st Century Themes		21 st Century Skills	
X	Global Awareness	E,T,A	Critical Thinking & Problem Solving	
	Environmental Literacy	E,T,A	Creativity and Innovation	
	Health Literacy	E,T,A	Collaboration, Teamwork and Leadership	
	Civic Literacy	E,T,A	Cross-Cultural and Interpersonal Communication	
X	Financial, Economic, Business and		Communication and Media Fluency	

	Entrepreneurial Literacy Accountability, Productivity and Ethics
In this unit plan,	the following Career Ready Practices are addressed:
Indicate whether	r these skills are E -Encouraged, T- Taught, or A -Assessed in this unit by marking E, T, A on the line before the appropriate skill.
Ⅱ	CRP1. Act as a responsible and contributing citizen and employee
E,T,A	CRP2. Apply appropriate academic and technical skills
╙	CRP3. Attend to personal health and financial well-being
E,T,A	CRP4. Communicate clearly and effectively with reason
E,T	CRP5. Consider the environmental, social and economic impacts of decisions
E,T,A	CRP6. Demonstrate creativity and innovation
E,T,A	CRP7. Employ valid and reliable research strategies
E,T,A	CRP8. Utilize critical thinking to make sense of problems and persevere in solving them

E E, T, A	CRP9. Model integrity, ethical leadership and effective management CRP10. Plan education and career paths aligned to personal goals CRP11. Use technology to enhance productivity
E,T	CRP12. Work productively in teams while using cultural global competence

Formative:

(Through what authentic performance tasks will students demonstrate the desired understandings? By what criteria will performances of understanding be judged?)

NOTE: The assessment models provided in this document are suggestions for the teacher. If the teacher chooses to develop his/her own model, it must be of equal or better quality and at the same or higher cognitive levels (as noted in parentheses).

Depending upon the needs of the class, the assessment questions may be answered in the form of essays, quizzes, mobiles, PowerPoint, oral reports, booklets, or other formats of measurement used by the teacher.

ACCC Math 220 – Lab #2
Case Study Rating Television Shows
Real Statistics – Real Decisions project

Summative Assessment Measures: (Through what other evidence (E.g. quizzes, tests, academic prompts, observations, homework, journals, etc.) will students demonstrate achievement of the desired results? How will students reflect upon and self- assess their learning?) ***Attach all Benchmarks

Suggested days of	Subject/Grade Level: 11/12	Unit 2 Descriptive Statistics
Instruction	Statistical Methods	Topic: The use of descriptive statistics as a tool
15 days		Overarching Goals:
		(1) Communicate mathematical ideas in clear, concise, organized language that varies in content, format and form for different audiences and purposes.
		(2) Comprehend, understand, analyze, evaluate, critique, solve, and respond to a variety of real-life, meaningful problems.
		(3) Investigate, research, and synthesize various information from a variety of media sources.
		Goal 2: The student will be able to organization and description of data sets to make data easier to understand by describing trends, averages, and variations
		Student Learning Outcome: Student will build frequency distributions and present statistical results graphically; Student will describe data with descriptive statistics
	Objectives / Cluster Concepts /	Essential Questions, Enduring Understandings, Sample Conceptual Understandings
	Cumulative Progress Indicators (CPI's)	
	The student will be able to:	

- 2.1. Frequency
 Distribution s-ID A-2
- 2.2. Graphs of Frequency Distributions (i.e. histogram, frequency polygon, ogive)

S-ID A-1

- 2.3a Electronic construction of graphs using frequency distributions s-ID A-1
- 2.3. Graphing Quantitative Data Sets (i.e. stemplot, dot plot)

S-ID A-1

2.4. Graphing Qualitative Data Sets (i.e. pie chart, Pareto)

S-ID B-5

- 2.4a Graphing Paired Data Sets (i.e. scatter plot, time series chart) s-ID
- 2.4b Mean, Median, Mode, Range s-ID A-2
- 2.5. Weighted Mean S-ID A-2
- 2.6. Distribution Shapes s-
- 2.7. Variance and Standard Deviation including the Interpretation s-ID A-4
- 2.8. Coefficient of Variation s-ID A-4
- 2.9. Creating and Applying Five Number Summary s-ID A-1-3
- 2.10. Standard Score s-ID A-4

Essential Questions:

- How do you organize and describe data sets?
- How do you graph and interpret quantitative data sets using histograms and ogives?
- How do you graph and interpret quantitative data sets using stem and dot plots?
- How do you graph and interpret qualitative data sets using pie charts and Pareto charts?
- How do you graph and interpret paired data sets using scatter plots and time series charts?
- How do you describe data with measures of central tendency, variation, and/or position?
- How do you interpret numerical descriptions of data sets?
- How do you find variance and standard deviation od a population and sample?
- How do you use coefficient of variation to compare variation in different data sets?
- How do you use quartiles to describe data sets?
- How do you interpret other fractals such as percentiles and how to find percentiles?
- How to find and interpret the standard score?

In this unit plan, the following 21st Century themes and skills are addressed:

2	Check all that apply. 21 st Century Themes		nether these skills are E -Encouraged, T- Taught, or A -Assessed in this unit by marking E, line before the appropriate skill. 21st Century Skills
X	Global Awareness	E,T,A	Critical Thinking & Problem Solving
	Environmental Literacy	E,T,A	Creativity and Innovation
	Health Literacy	E,T,A	Collaboration, Teamwork and Leadership
	Civic Literacy	E,T,A	Cross-Cultural and Interpersonal Communication
X	Financial, Economic, Business and		Communication and Media Fluency
	Entrepreneurial Literacy		Accountability, Productivity and Ethics
this unit plan,	, the following Career Ready Practices are	e addressed:	
ndicate whethe	r these skills are E -Encouraged, T- Taught, or A	N-Assessed in t	his unit by marking E, T, A on the line before the appropriate skill.
	CRP1. Act as a responsible and contri	ibuting citize	en and employee
E,T,A	CRP2. Apply appropriate academic and technical skills		
	CRP3. Attend to personal health and financial well-being		
E,T,A	CRP4. Communicate clearly and effectively with reason		
E,T	CRP5. Consider the environmental, social and economic impacts of decisions		
E,T,A	CRP6. Demonstrate creativity and innovation		
E,T,A	CRP7. Employ valid and reliable research strategies		
E,T,A	CRP8. Utilize critical thinking to make sense of problems and persevere in solving them		

E E, T, A	CRP9. Model integrity, ethical leadership and effective management CRP10. Plan education and career paths aligned to personal goals
E,T	CRP11. Use technology to enhance productivity CRP12. Work productively in teams while using cultural global competence

Formative:

(Through what authentic performance tasks will students demonstrate the desired understandings? By what criteria will performances of understanding be judged?)

NOTE: The assessment models provided in this document are suggestions for the teacher. If the teacher chooses to develop his/her own model, it must be of equal or better quality and at the same or higher cognitive levels (as noted in parentheses).

Depending upon the needs of the class, the assessment questions may be answered in the form of essays, quizzes, mobiles, PowerPoint, oral reports, booklets, or other formats of measurement used by the teacher.

ACCC Math 220 – Lab #1 Case Study Business Size Real Statistics – Real Decisions project **Summative Assessment Measures:** (Through what other evidence (E.g. quizzes, tests, academic prompts, observations, homework, journals, etc.) will students demonstrate achievement of the desired results? How will students reflect upon and self- assess their learning?) ***Attach all Benchmarks

Suggested days of Instruction	Subject/Grade Level: 11/12	Unit 3 Probability Introduction Topic: Applying basic probability to various events
15 days	Statistical Methods	Overarching Goals: (1) Communicate mathematical ideas in clear, concise, organized language that varies in content, format and form for different audiences and purposes. (2) Comprehend, understand, analyze, evaluate, critique, solve, and respond to a variety of real-life, meaningful problems. (3) Investigate, research, and synthesize various information from a variety of media sources. Goal 3: The student will be able to determine the probability of an event. Student Learning Outcome: Student will apply counting techniques to probability and discrete probability distributions
	Objectives / Cluster Concepts / Cumulative Progress Indicators (CPI's) The student will be able to:	Essential Questions, Enduring Understandings, Sample Conceptual Understandings

3.	1. Probability Experiments s-CP A-1	Essential Questions: How do you determine sample space?
3.2	2. The Fundamental Counting Experiment S-CP B-1	How do you use the Fundamental Counting Principle? How do you find and apply classical, subjective, and experimental probability?
3.3	3. Classical, Subjective, Experimental Probability s-CP A-1	How do you find conditional probability? How do you find and apply Addition and Multiplication Rule for probability? When and how do you use permutations and combinations?
3.4	 Complementary Events 	
3.9	5. Conditional Probability s-CP A-3	
3.0	6. Independent and Dependent Events s- CP A-2	
3.	7. The Multiplication Rule s-CP B-8	
3.8	B. The Addition Rule s- CP B-7	
3.9	9. Permutations s-CP B-9	
3.	10. Combinations s-CP B-9	
3.4	11. Applications of Probability s-MD B-5-7	

Check all that apply. 21 st Century Themes		Indicate whether these skills are E -Encouraged, T -Taught, or A -Assessed in this unit by marking E , T , A on the line before the appropriate skill. 21 st Century Skills		
X	Global Awareness		E,T,A	Critical Thinking & Problem Solving
	Environmental Literacy		E,T,A	Creativity and Innovation
	Health Literacy		E,T,A	Collaboration, Teamwork and Leadership
	Civic Literacy		E,T,A	Cross-Cultural and Interpersonal Communication
X	Financial, Economic, Business and			Communication and Media Fluency

	Entrepreneurial Literacy Accountability, Productivity and Ethics						
In this unit plan, t	n this unit plan, the following Career Ready Practices are addressed:						
Indicate whether	Indicate whether these skills are E -Encouraged, T -Taught, or A -Assessed in this unit by marking E , T , A on the line before the appropriate skill.						
	CRP1. Act as a responsible and contributing citizen and employee						
E,T,A	CRP2. Apply appropriate academic and technical skills						
	CRP3. Attend to personal health and financial well-being						
E,T,A	CRP4. Communicate clearly and effectively with reason						
E,T	CRP5. Consider the environmental, social and economic impacts of decisions						
E,T,A	CRP6. Demonstrate creativity and innovation						
E,T,A	CRP7. Employ valid and reliable research strategies						
E,T,A	CRP8. Utilize critical thinking to make sense of problems and persevere in solving them						

E E, T, A	CRP9. Model integrity, ethical leadership and effective management CRP10. Plan education and career paths aligned to personal goals CRP11. Use technology to enhance productivity
E,T	CRP12. Work productively in teams while using cultural global competence
F	E, T, A

Formative:

(Through what authentic performance tasks will students demonstrate the desired understandings? By what criteria will performances of understanding be judged?)

NOTE: The assessment models provided in this document are suggestions for the teacher. If the teacher chooses to develop his/her own model, it must be of equal or better quality and at the same or higher cognitive levels (as noted in parentheses).

Depending upon the needs of the class, the assessment questions may be answered in the form of essays, quizzes, mobiles, PowerPoint, oral reports, booklets, or other formats of measurement used by the teacher.

ACCC Math 220 – Lab #3

Free Throw Outcome Probability Activity Case Study: United States Congress

Real Statistics-Real Decisions

Summative Assessment Measures: (Through what other evidence (E.g. quizzes, tests, academic prompts, observations, homework, journals, etc.) will students demonstrate achievement of the desired results? How will students reflect upon and self- assess their learning?) ***Attach all Benchmarks

Lesson Quizzes Unit Test

Suggested days of	Subject/Grade Level: 11/12	Unit 4 Discrete Probability Distributions				
Instruction Statistical Methods		Topic: Creating and using probability distributions				
22 days		 Overarching Goals: (1) Communicate mathematical ideas in clear, concise, organized language that varies in content, format and form for different audiences and purposes. (2) Comprehend, understand, analyze, evaluate, critique, solve, and respond to a variety of real-life, meaningful problems. (3) Investigate, research, and synthesize various information from a variety of media sources. 				
		Goal 4: The student will be able to create and use probability distributions. Student Learning Outcome: Student will construct and employ confidence intervals				
	Objectives / Cluster Concepts /	Essential Questions, Enduring Understandings, Sample Conceptual Understandings				
	Cumulative Progress Indicators (CPI's)	Sample Conceptual Onderstandings				
	The student will be able to:					

	4.1.4.2.4.3.4.4.4.5.4.6.4.7.4.8.4.9.	Random Variables s-MD A-1 Discrete Probability Distributions s-MD A-1 Mean, Variance, and Standard Deviation s-MD A-2 Expected Value s-MD A-2, 3, 4 Binomial Experiments Binomial Probability Formula Using technology to find Binomial Probabilities Graphing Binomial Distributions Population Parameters of Binomial Distribution	Essential Questions: How do you construct and graph discrete probability distributions? How do you find the mean, variance, and standard deviation of a discrete probability distribution? How do find expected value of a discrete probability distribution? How do you find binomial probabilities using, formulas, table, and technology? How do you construct and graph a binomial distribution? How do you find the mean, variance, and standard deviation of a binomial probability distribution?
--	--	--	---

In this unit plan, the following 21 st Century themes and sl Check all that apply.		Indicate whether these skills are E -Encouraged, T -Taught, or A -Assessed in this unit by marking E , T , A on the line before the appropriate skill.			
2	1 st Century Themes		21 st Century Skills		
X	Global Awareness	E,T,A	Critical Thinking & Problem Solving		
	Environmental Literacy	E,T,A	Creativity and Innovation		
	Health Literacy	E,T,A	Collaboration, Teamwork and Leadership		
	Civic Literacy	E,T,A	Cross-Cultural and Interpersonal Communication		
X	Financial, Economic, Business and		Communication and Media Fluency		

	Entrepreneurial Literacy		Accountability, Productivity and Ethics					
In this unit plan, th	n this unit plan, the following Career Ready Practices are addressed:							
Indicate whether t	Indicate whether these skills are E -Encouraged, T -Taught, or A -Assessed in this unit by marking E, T, A on the line before the appropriate skill.							
	CRP1. Act as a responsible and contributing citizen and employee							
E,T,A	CRP2. Apply appropriate academic and technical skills							
II	CRP3. Attend to personal health and financial well-being							
E,T,A	CRP4. Communicate clearly and effectively with reason							
E,T	CRP5. Consider the environmental, social and economic impacts of decisions							
E,T,A	CRP6. Demonstrate creativity and innovation							
E,T,A	CRP7. Employ valid and reliable research strategies							
E,T,A	CRP8. Utilize critical thinking to make sense of problems and persevere in solving them							

E E, T, A	CRP9. Model integrity, ethical leadership and effective management CRP10. Plan education and career paths aligned to personal goals CRP11. Use technology to enhance productivity
E,T	CRP12. Work productively in teams while using cultural global competence

Formative:

(Through what authentic performance tasks will students demonstrate the desired understandings? By what criteria will performances of understanding be judged?)

NOTE: The assessment models provided in this document are suggestions for the teacher. If the teacher chooses to develop his/her own model, it must be of equal or better quality and at the same or higher cognitive levels (as noted in parentheses).

Depending upon the needs of the class, the assessment questions may be answered in the form of essays, quizzes, mobiles, PowerPoint, oral reports, booklets, or other formats of measurement used by the teacher.

ACCC Math 220 - Lab #4

Case Study Distribution of hit in baseball games

Real Statistics - Real Decisions project

Summative Assessment Measures: (Through what other evidence (E.g. quizzes, tests, academic prompts, observations, homework, journals, etc.) will students demonstrate achievement of the desired results? How will students reflect upon and self- assess their learning?) ***Attach all Benchmarks

Lesson Quizzes Unit Test

Suggested days of	Subject/Grade Level: 11/12	Unit 5 Normal Probability Distributions
Instruction	Statistical Methods	Topic: Normal Distribution Curves and use of their properties
23 days		Overarching Goals:
		(1) Communicate mathematical ideas in clear, concise, organized language that varies in content, format and form for different audiences and purposes.
		(2) Comprehend, understand, analyze, evaluate, critique, solve, and respond to a variety of real-life, meaningful problems.
		(3) Investigate, research, and synthesize various information from a variety of media sources.
		Goal 5: The student will be able to recognize normal distributions and apply their properties to real-life situations.
		Student Learning Outcome: Student will apply the Normal distribution, confidence intervals, sample size, hypothesis testing, analysis of variance, correlation, and regressio nto obtain statistical results with which they will draw conclusions.
	Objectives / Cluster Concepts /	Essential Questions, Enduring Understandings, Sample Conceptual Understandings
	Cumulative Progress Indicators (CPI's)	
	The student will be able to:	

5.1.	Properties of a	Essential Questions:
	Normal Distribution s-	How do you interpret graphs of normal probability distributions?
5.2.	Standard Normal	How do find area under the standard normal curve?
	Distribution Area s-ID A-	How do find probabilities for normal distributions using a table and technology?
5.3.	Application of Normal	How do you find z-score and transform it to an x-value?
0.0.	Distribution S-ID A-4	How do you apply normal distribution to find data?
5.4.	Probability for Normal	How do you find and verify sampling distribution?
	Distributions S-ID A-4	How do you interpret the Central Limit Theorem?
5.5.	Finding and applying Z-score S-ID A-4	How do you apply the Central Limit Theorem to find the probability of a sample mean?
5.6.	Sampling distributions S-MD A-3	
5.7.	The Central Limit	
	Theorem	

	Check all that apply. 21 st Century Themes		Indicate whether these skills are E -Encouraged, T -Taught, or A -Assessed in this unit by marking E , T , A on the line before the appropriate skill. 21 st Century Skills		
X	Global Awareness		E,T,A	Critical Thinking & Problem Solving	
	Environmental Literacy		E,T,A	Creativity and Innovation	
	Health Literacy		E,T,A	Collaboration, Teamwork and Leadership	
	Civic Literacy		E,T,A	Cross-Cultural and Interpersonal Communication	
X	Financial, Economic, Business and			Communication and Media Fluency	

	Entrepreneurial Literacy		Accountability, Productivity and Ethics		
In this unit plan, tl	ne following Career Ready Practices are a	addressed:			
Indicate whether t	hese skills are E -Encouraged, T- Taught, or A -A	Assessed in tl	nis unit by marking E, T, A on the line before the appropriate skill.		
	CRP1. Act as a responsible and contrib	uting citize	n and employee		
E,T,A	CRP2. Apply appropriate academic an	d technical	skills		
	CRP3. Attend to personal health and financial well-being				
E,T,A	CRP4. Communicate clearly and effectively with reason				
E,T	CRP5. Consider the environmental, soo	cial and eco	nomic impacts of decisions		
E,T,A	CRP6. Demonstrate creativity and inne	ovation			
E,T,A	CRP7. Employ valid and reliable research strategies				
E,T,A	CRP8. Utilize critical thinking to make	sense of pr	oblems and persevere in solving them		

E E, T, A	CRP9. Model integrity, ethical leadership and effective management CRP10. Plan education and career paths aligned to personal goals CRP11. Use technology to enhance productivity
E,T	CRP12. Work productively in teams while using cultural global competence

Formative:

(Through what authentic performance tasks will students demonstrate the desired understandings? By what criteria will performances of understanding be judged?)

NOTE: The assessment models provided in this document are suggestions for the teacher. If the teacher chooses to develop his/her own model, it must be of equal or better quality and at the same or higher cognitive levels (as noted in parentheses).

Depending upon the needs of the class, the assessment questions may be answered in the form of essays, quizzes, mobiles, PowerPoint, oral reports, booklets, or other formats of measurement used by the teacher.

ACCC Math 220 – Lab #3

Case Study: Birth Weights in America Real Statistics – Real Decisions project

Summative Assessment Measures: (Through what other evidence (E.g. quizzes, tests, academic prompts, observations, homework, journals, etc.) will students demonstrate achievement of the desired results? How will students reflect upon and self- assess their learning?) ***Attach all Benchmarks

Suggested days of	Subject/Grade Level: 11/12	Unit 6 Confidence Intervals
Instruction	Statistical Methods	Topic: Confidence Intervals when σ is known, unknown, and population proportions
15 days		Overarching Goals:
		(1) Communicate mathematical ideas in clear, concise, organized language that varies in content, format and form for different audiences and purposes.
		(2) Comprehend, understand, analyze, evaluate, critique, solve, and respond to a variety of real-life, meaningful problems.
		(3) Investigate, research, and synthesize various information from a variety of media sources.
		Goal 6: The student will be able to make a meaningful estimate by specifying an interval of values on a number line, together with a statement of how confident you are that your interval contains the population parameter.
		Student Learning Outcome: Student will construct and employ confidence intervals.
	Objectives / Cluster Concepts /	Essential Questions, Enduring Understandings, Sample Conceptual Understandings
	Cumulative Progress Indicators (CPI's)	
	The student will be able to:	

6.1. 6.2.	Estimation Population Parameter s-IC A, B Confidence Intervals	Essential Questions: What is inferential statistics?
0.2.	for a Population Mean	How do you find point estimate and margin of error? How do you construct and interpret confidence intervals for a population mean when σ is known?
6.3.	Finding Minimum Sample Size to Estimate the Population S-IC B-3-4	How do you determine the minimum sample size required when estimating a population sample size? How do you construct and interpret confidence intervals for a population mean when σ is unknown? How do you construct and interpret confidence intervals for a population proportion?
6.4.	Confidence Intervals and t-distribution s-IC B	How to determine the minimum sample size required when estimation a population proportion?
6.5.	Confidence Intervals for Population Proportions S-IC B-4, 6	

2	Check all that apply. 21 st Century Themes		Indicate whether these skills are E -Encouraged, T -Taught, or A -Assessed in this unit by marking E , T , A on the line before the appropriate skill. 21 st Century Skills		
X	Global Awareness		E,T,A	Critical Thinking & Problem Solving	
	Environmental Literacy		E,T,A	Creativity and Innovation	
	Health Literacy		E,T,A	Collaboration, Teamwork and Leadership	
	Civic Literacy		E,T,A	Cross-Cultural and Interpersonal Communication	
X	Financial, Economic, Business and			Communication and Media Fluency	

	Entrepreneurial Literacy		Accountability, Productivity and Ethics				
In this unit plan, tl	n this unit plan, the following Career Ready Practices are addressed:						
Indicate whether t	hese skills are E -Encouraged, T -Taught, or A -A	Assessed in ti	his unit by marking E, T, A on the line before the appropriate skill.				
	CRP1. Act as a responsible and contrib	uting citize	n and employee				
E,T,A	CRP2. Apply appropriate academic an	d technical	skills				
	CRP3. Attend to personal health and financial well-being						
E,T,A	CRP4. Communicate clearly and effectively with reason						
E,T	CRP5. Consider the environmental, so	cial and eco	nomic impacts of decisions				
E,T,A	CRP6. Demonstrate creativity and inn	ovation					
E,T,A	CRP7. Employ valid and reliable research strategies						
E,T,A	CRP8. Utilize critical thinking to make	sense of pr	oblems and persevere in solving them				

CRP9. Model integrity, ethical leadership and effective management CRP10. Plan education and career paths aligned to personal goals CRP11. Use technology to enhance productivity
CRP12. Work productively in teams while using cultural global competence

Formative:

(Through what authentic performance tasks will students demonstrate the desired understandings? By what criteria will performances of understanding be judged?)

NOTE: The assessment models provided in this document are suggestions for the teacher. If the teacher chooses to develop his/her own model, it must be of equal or better quality and at the same or higher cognitive levels (as noted in parentheses).

Depending upon the needs of the class, the assessment questions may be answered in the form of essays, quizzes, mobiles, PowerPoint, oral reports, booklets, or other formats of measurement used by the teacher.

ACCC Math 220 – Lab #3

Case Study: Marathon Training Real Statistics – Real Decisions project **Summative Assessment Measures:** (Through what other evidence (E.g. quizzes, tests, academic prompts, observations, homework, journals, etc.) will students demonstrate achievement of the desired results? How will students reflect upon and self- assess their learning?) ***Attach all Benchmarks

Suggested days of	Subject/Grade Level: 11/12	Unit 7 Hypothesis Testing with One Sample
Instruction 15 days	Statistical Methods	Topic: Hypothesis Testing for Mean (σ known and unknown), Proportions, Variance and Standard Deviations Overarching Goals:
		(1) Communicate mathematical ideas in clear, concise, organized language that varies in content, format and form for different audiences and purposes.
		(2) Comprehend, understand, analyze, evaluate, critique, solve, and respond to a variety of real-life, meaningful problems.
		(3) Investigate, research, and synthesize various information from a variety of media sources.
		Goal 7: The student will be able to test a claim about a parameter.
		Student Learning Outcome: Student will construct and employ confidence intervals
		Student Learning Outcome: Student will apply the Normal distribution, confidence intervals, sample size, hypothesis testing, analysis of variance, correlation, and regressio nto obtain statistical results with which they will
		draw conclusions.
	Objectives / Cluster Concepts /	Essential Questions, Enduring Understandings, Sample Conceptual Understandings
	Cumulative Progress Indicators (CPI's)	
	The student will be able to:	

7.	1. Hypothesis Test Terminology s-ic B	Essential Questions: What is a hypothesis test?
7	2. Stating a a Hypothesis s-ICB	How do you state a hypothesis? What are error types and interpret the level of significance?
7.	3. Types of Errors and Level of Significance	When do you use one-tail or tow-tailed statistical test and find <i>p</i> -value? How do you make and interpret a decision based on the results of a statistical test?
7.	 Statistical Test and P- Values 	How do you find and interpret P -values? How do you use P -values for a z -test for a mean when μ and σ is known?
7.	5. Decision Rule Based on <i>P</i> -Value	How to find critical values and rejection regions of a standard normal distribution?
7.	 Hypothesis Testing for the Mean with Known Population Standard Deviation 	How to use rejection regions for a <i>z</i> -test for a mean μ when σ is known? How do you use <i>z</i> -test to test a population proportion?
7.	 Hypothesis Testing for the Mean with Unknown Population Standard Deviation 	
7.	Hypothesis Test for Proportions	
7.	9. Hypothesis Test for Variance and Standard Deviation	

In this unit plan, the following 21st Century themes and s Check all that apply. 21st Century Themes		Indicate whether these skills are E-Encouraged, T-Taught, or A-Assessed in this unit by marking E, T, A on the line before the appropriate skill. 21 st Century Skills		
X	Global Awareness		E,T,A	Critical Thinking & Problem Solving
	Environmental Literacy		E,T,A	Creativity and Innovation
	Health Literacy		E,T,A	Collaboration, Teamwork and Leadership
	Civic Literacy		E,T,A	Cross-Cultural and Interpersonal Communication
X	Financial, Economic, Business and			Communication and Media Fluency

	Entrepreneurial Literacy	Accountability, Productivity and Ethics	
In this unit plan, t	he following Career Ready Practices are a	ddressed:	
Indicate whether	these skills are E -Encouraged, T- Taught, or A -As	ssessed in this unit by marking E, T, A on the line before the appropriate skill.	
	CRP1. Act as a responsible and contribu	iting citizen and employee	
E,T,A	CRP2. Apply appropriate academic and	technical skills	
Ⅱ —	CRP3. Attend to personal health and financial well-being		
E,T,A	CRP4. Communicate clearly and effecti	vely with reason	
E,T	CRP5. Consider the environmental, soci	al and economic impacts of decisions	
E,T,A	CRP6. Demonstrate creativity and inno	vation	
E,T,A	CRP7. Employ valid and reliable researd	ch strategies	
E,T,A	CRP8. Utilize critical thinking to make so	ense of problems and persevere in solving them	

E E, T, A	CRP9. Model integrity, ethical leadership and effective management CRP10. Plan education and career paths aligned to personal goals CRP11. Use technology to enhance productivity
E,T	CRP12. Work productively in teams while using cultural global competence

Formative:

(Through what authentic performance tasks will students demonstrate the desired understandings? By what criteria will performances of understanding be judged?)

NOTE: The assessment models provided in this document are suggestions for the teacher. If the teacher chooses to develop his/her own model, it must be of equal or better quality and at the same or higher cognitive levels (as noted in parentheses).

Depending upon the needs of the class, the assessment questions may be answered in the form of essays, quizzes, mobiles, PowerPoint, oral reports, booklets, or other formats of measurement used by the teacher.

ACCC Math 220 - Lab #4

Case Study: Human Body Temperature What's Normal

Real Statistics - Real Decisions project

Summative Assessment Measures: (Through what other evidence (E.g. quizzes, tests, academic prompts, observations, homework, journals, etc.) will students demonstrate achievement of the desired results? How will students reflect upon and self- assess their learning?) ***Attach all Benchmarks

Lesson Quizzes Unit Test

Suggested days of Subject/Grade Level: 11/1		Unit 8 Hypothesis Testing with Two Samples
Instruction	Statistical Methods	Topic:
15 days		Overarching Goals:
		(1) Communicate mathematical ideas in clear, concise, organized language that varies in content, format and form for different audiences and purposes.
		(2) Comprehend, understand, analyze, evaluate, critique, solve, and respond to a variety of real-life, meaningful problems.
		(3) Investigate, research, and synthesize various information from a variety of media sources.
		Goal 8: The student will be able to test a hypothesis that compares two populations. Student Learning Outcome: Student will apply the Normal distribution, confidence intervals, sample size, hypothesis testing, analysis of variance, correlation, and regressio nto obtain statistical results with which they will draw conclusions.
	Objectives / Cluster Concepts /	Essential Questions, Enduring Understandings, Sample Conceptual Understandings
	Cumulative Progress Indicators (CPI's)	
	The student will be able to:	

8.1. Independent and Dependent Samples 8.2. Two-Sample z-Test for the Difference Between Means	 Essential Questions: How do you determine whether two samples are independent or dependent? How do you perform a two-sample z-test for the difference between two means using independent samples σ₁ and σ₂ known? How to hypothesis test for a difference between two variances?
8.3. Testing the Difference Between Two Variances	How to hypothesis test for a difference between two variances?

Check all that apply. 21 st Century Themes		Indicate whether these skills are E -Encouraged, T -Taught, or A -Assessed in this unit by marking E , T , A on the line before the appropriate skill. 21 st Century Skills		
X	Global Awareness		E,T,A	Critical Thinking & Problem Solving
	Environmental Literacy		E,T,A	Creativity and Innovation
	Health Literacy		E,T,A	Collaboration, Teamwork and Leadership
	Civic Literacy		E,T,A	Cross-Cultural and Interpersonal Communication
X	Financial, Economic, Business and			Communication and Media Fluency

	Entrepreneurial Literacy		Accountability, Productivity and Ethics					
In this unit plan, tl	n this unit plan, the following Career Ready Practices are addressed:							
Indicate whether t	hese skills are E -Encouraged, T- Taught, or A -A	Assessed in tl	nis unit by marking E, T, A on the line before the appropriate skill.					
	CRP1. Act as a responsible and contrib	outing citize	n and employee					
E,T,A	CRP2. Apply appropriate academic an	d technical	skills					
Ⅱ —	CRP3. Attend to personal health and financial well-being							
E,T,A	CRP4. Communicate clearly and effectively with reason							
E,T	CRP5. Consider the environmental, so	cial and eco	nomic impacts of decisions					
E,T,A	CRP6. Demonstrate creativity and inn	ovation						
E,T,A	CRP7. Employ valid and reliable resea	rch strategi	es					
E,T,A	CRP8. Utilize critical thinking to make	sense of pr	oblems and persevere in solving them					

E E, T	Г, А	CRP9. Model integrity, ethical leadership and effective management CRP10. Plan education and career paths aligned to personal goals CRP11. Use technology to enhance productivity
E,T	Т	CRP12. Work productively in teams while using cultural global competence

Formative:

(Through what authentic performance tasks will students demonstrate the desired understandings? By what criteria will performances of understanding be judged?)

NOTE: The assessment models provided in this document are suggestions for the teacher. If the teacher chooses to develop his/her own model, it must be of equal or better quality and at the same or higher cognitive levels (as noted in parentheses).

Depending upon the needs of the class, the assessment questions may be answered in the form of essays, quizzes, mobiles, PowerPoint, oral reports, booklets, or other formats of measurement used by the teacher.

ACCC Math 220 - Lab #4

Real Statistics – Real Decisions project

Case Study: How Protein Affects Weight Gain in Overeaters

Summative Assessment Measures: (Through what other evidence (E.g. quizzes, tests, academic prompts, observations, homework, journals, etc.) will students demonstrate achievement of the desired results? How will students reflect upon and self- assess their learning?) ***Attach all Benchmarks

Lesson Quizzes Unit Test

Suggested days of Instruction	Subject/Grade Level: 11/12	Unit 9 Correlation and Regression Topic: Correlation, Regression, and Prediction Intervals
		10pior 001101ano11, 110gi 0001011, and 1110ano11011 miles valo
22 days	Statistical Methods	 Overarching Goals: (1) Communicate mathematical ideas in clear, concise, organized language that varies in content, format and form for different audiences and purposes. (2) Comprehend, understand, analyze, evaluate, critique, solve, and respond to a variety of real-life, meaningful problems. (3) Investigate, research, and synthesize various information from a variety of media sources.
		Goal 9: The student will be able to calculate and apply properties of correlation and regression to real-life problems. Student Learning Outcome: Student will apply the normal distribution, confidence intervals, sample size, hypothesis testing, analysis of variance, correlation, and regression to obtain statistical results with which they will draw conclusions
	Objectives / Cluster Concepts /	Essential Questions, Enduring Understandings, Sample Conceptual Understandings
	Cumulative Progress Indicators (CPI's)	
	The student will be able to:	

(9.1. Correlation	Essential Questions:
	Introduction S-ID B-5	What is correlation and types of correlation?
	9.2. Correlation	How do you find correlation coefficient?
	Coefficient s-ID B-5-6, C	How do you test a population correlation coefficient ρ using a table?
	9.3. Test a Population Correlation	How to perform a hypothesis test for a population correlation coefficient?
	Coefficient S-ID B-5, C-8	How do you determine between correlation and causation?
	9.4. Hypothesis Testing	How do you find the equation of a regression line?
	for a Population	How do you predict y-values using a regression equation?
	Correlation Coefficient s-ID B-5, 6, C	How to interpret the three types of variation about a regression line?
	9.5. Correlation and	How to find and interpret the coefficient of determination?
	Causation s-ID C-9	How to find and interpret the standard error of estimate for a regression line?
	9.6. Regression Lines a	nd How to construct and interpret a prediction interval for y?
	their Application S-ID	
	9.7. Variation of a	How to use multiple regression to predict <i>y</i> -values?
	Regression Line s-ID	В-
(9.8. Coefficient of	
	Determination s-ID C-8	
	9.9. Standard Error of Estimate s-ID C-8	
(9.10. Prediction Intervals	S-
	9.11. Multiple Regression Equations	
	9.12. Prediction <i>y</i> -Values	S-

In this unit plan, the following 21 st Century themes and skills are addressed:					
Check all that apply.		Indicate whether these skills are E -Encouraged, T -Taught, or A -Assessed in this unit by marking E , T , A on the line before the appropriate skill.			
21 st Century Themes		21 st Century Skills			
X Global Awareness		,T,A	Critical Thinking & Problem Solving		
Environmental Literacy	E,	,T,A	Creativity and Innovation		

X	Health Literacy Civic Literacy Financial, Economic, Business and Entrepreneurial Literacy	E,T,A E,T,A	Collaboration, Teamwork and Leadership Cross-Cultural and Interpersonal Communication Communication and Media Fluency Accountability, Productivity and Ethics	
In this unit pl	lan, the following Career Ready Practices are	addressed:		
Indicate whe	ther these skills are E -Encouraged, T- Taught, or A -	Assessed in t	his unit by marking E, T, A on the line before the appropriate skill.	
	CRP1. Act as a responsible and contrib	outing citize	n and employee	
E,T,A	CRP2. Apply appropriate academic an	CRP2. Apply appropriate academic and technical skills		
	CRP3. Attend to personal health and f	CRP3. Attend to personal health and financial well-being		
E,T,A	CRP4. Communicate clearly and effec	CRP4. Communicate clearly and effectively with reason		
E,T	CRP5. Consider the environmental, so	CRP5. Consider the environmental, social and economic impacts of decisions		
E,T,A	CRP6. Demonstrate creativity and inn	CRP6. Demonstrate creativity and innovation		
E,T,A	CRP7. Employ valid and reliable resea	CRP7. Employ valid and reliable research strategies		
E,T,A	CRP8. Utilize critical thinking to make	CRP8. Utilize critical thinking to make sense of problems and persevere in solving them		

E E, T, A	CRP9. Model integrity, ethical leadership and effective management CRP10. Plan education and career paths aligned to personal goals CRP11. Use technology to enhance productivity
E,T	CRP12. Work productively in teams while using cultural global competence

Formative:

(Through what authentic performance tasks will students demonstrate the desired understandings? By what criteria will performances of understanding be judged?)

NOTE: The assessment models provided in this document are suggestions for the teacher. If the teacher chooses to develop his/her own model, it must be of equal or better quality and at the same or higher cognitive levels (as noted in parentheses).

Depending upon the needs of the class, the assessment questions may be answered in the form of essays, quizzes, mobiles, PowerPoint, oral reports, booklets, or other formats of measurement used by the teacher.

ACCC Math 220 – Lab #5 Real Statistics – Real Decisions project **Summative Assessment Measures:** (Through what other evidence (E.g. quizzes, tests, academic prompts, observations, homework, journals, etc.) will students demonstrate achievement of the desired results? How will students reflect upon and self- assess their learning?) ***Attach all Benchmarks

Suggested	Subject/Grade Level: 11/12	Unit 10 Chi-Square
days of Instruction	Statistical Methods	Unit 10 Topic: Chi-square and Analysis of Variance (ANOVA)
23 days		Overarching Goals:
		(1) Communicate mathematical ideas in clear, concise, organized language that varies in content, format and form for different audiences and purposes.
		(2) Comprehend, understand, analyze, evaluate, critique, solve, and respond to a variety of real-life, meaningful problems.
		(3) Investigate, research, and synthesize various information from a variety of media sources.
		Goal 10: The student will be able to use ANOVA to determine if there is a significant difference among three or more means.
		Student learning outcomes: Student will apply the normal distribution, confidence intervals, sample size, hypothesis testing, analysis of variance, correlation, and regression to obtain statistical results with which they will draw conclusions; Student will use technology to help solve problems, experiment, analysis results, interpret results, and verify conclusions
	Objectives / Cluster	Essential Questions, Enduring Understandings,
	Concepts /	Sample Conceptual Understandings
	Cumulative Progress Indicators (CPI's)	
	The student will be able to:	

In this unit plan, the following 21st Century themes and s Check all that apply.		Indicate whether these skills are E -Encouraged, T -Taught, or A -Assessed in this unit by marking E , T , A on the line before the appropriate skill.		
21 st Century Themes		21 st Century Skills		
X	Global Awareness		E,T,A	Critical Thinking & Problem Solving
	Environmental Literacy		E,T,A	Creativity and Innovation
	Health Literacy		E,T,A	Collaboration, Teamwork and Leadership
	Civic Literacy		E,T,A	Cross-Cultural and Interpersonal Communication
X	Financial, Economic, Business and			Communication and Media Fluency

	Entrepreneurial Literacy		Accountability, Productivity and Ethics				
In this unit plan,	this unit plan, the following Career Ready Practices are addressed:						
Indicate whethe	r these skills are E -Encouraged, T -Taught, or A	-Assessed in t	his unit by marking E, T, A on the line before the appropriate skill.				
	CRP1. Act as a responsible and contributing citizen and employee						
E,T,A	CRP2. Apply appropriate academic and technical skills						
I	CRP3. Attend to personal health and financial well-being						
E,T,A	CRP4. Communicate clearly and effectively with reason						
E,T	CRP5. Consider the environmental, social and economic impacts of decisions						
E,T,A	CRP6. Demonstrate creativity and innovation						
E,T,A	CRP7. Employ valid and reliable research strategies						
E,T,A	CRP8. Utilize critical thinking to make sense of problems and persevere in solving them						

E E, T, A	CRP9. Model integrity, ethical leadership and effective management CRP10. Plan education and career paths aligned to personal goals CRP11. Use technology to enhance productivity
E,T	CRP12. Work productively in teams while using cultural global competence

Formative:

(Through what authentic performance tasks will students demonstrate the desired understandings? By what criteria will performances of understanding be judged?)

NOTE: The assessment models provided in this document are suggestions for the teacher. If the teacher chooses to develop his/her own model, it must be of equal or better quality and at the same or higher cognitive levels (as noted in parentheses).

Depending upon the needs of the class, the assessment questions may be answered in the form of essays, quizzes, mobiles, PowerPoint, oral reports, booklets, or other formats of measurement used by the teacher.

ACCC Math 220 – Lab #6
Real Statistics – Real Decisions project
Case Study: Food Safety Survey

Summative Assessment Measures: (Through what other evidence (E.g. quizzes, tests, academic prompts, observations, homework, journals, etc.) will students demonstrate achievement of the desired results? How will students reflect upon and self- assess their learning?) ***Attach all Benchmarks

Modifications

Additional considerations for English Language Learners (ELLs), Special Needs, Below Level (BSI)

Individualized Education Plans (IEPs):

- ⇒ Exemplars of varied performance levels
- ⇒ Multi-media presentations Consultation with ESL teachers
- ⇒ Manipulatives
- ⇒ Tiered/Scaffolded Lessons
- ⇒ Mnemonic devices
- ⇒ Visual aids
- \Rightarrow Modeling
- ⇒ Guided note-taking
- ⇒ Study Guides
- ⇒ Modified homework
- ⇒ Differentiated pre-typed class notes and example problems

Advanced/Gifted Students:

- ⇒ Open-ended responses
- ⇒ Curriculum Compacting
- ⇒ Advanced problems to extend the critical thinking skills of advanced learner
- ⇒ Supplemental reading material for independent study
- \Rightarrow Flexible grouping
- ⇒ Tiered assignments

Resources

Elementary Statistics: Picturing the world

Supplemental Material from The Practice of Statistics